

USING LATTICE TOPOLOGY INFORMATION TO INVESTIGATE PERSISTENT SCATTERERS AT FACADES IN URBAN AREAS

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Commission VII/2

KEY WORDS: High resolution, SAR, Urban, Pattern, Data, Fusion

ABSTRACT:

Modern spaceborne SAR sensors like TerraSAR-X offer ground resolution of up to one meter in range and azimuth direction. Buildings, roads, bridges, and other man-made structures appear in such data often as regular patterns of strong and temporally stable points (Persistent Scatterer, PS). As one step in the process of unveiling what object structure actually causes the PS (i.e., physical nature) we compare those regular structures in SAR data to their correspondences in optical imagery. We use lattices as a common data representation for visible facades. By exploiting the topology information given by the lattices we can complete gaps in the structures which is one step towards the understanding of the complex scattering characteristics of distinct facade objects.

1 INTRODUCTION

The most prominent motivation for the fusion of SAR and optical data is the combination of the advantages of both sensor types. A combined data analysis promises the weather independence of SAR with the high-resolution and straightforward interpretability of airborne optical imagery. Also the broad field of change detection or natural disaster management offer many applications for a methodology of fusing SAR and optical data. Due to the oblique sensing geometry, especially facades are visible in SAR acquisitions as well as in oblique aerial imagery considering urban areas. Since modern spaceborne SAR sensors like TerraSAR-X or CosmoSkyMed offer ground resolutions of up to one meter in range and azimuth direction, facade objects like single windows or balconies can be distinguished as separate Persistent Scatterers. Those points are temporally stable and do have a dominant contribution to the signal of it's resolution cell (Ferretti et al., 2001). Many of those PS exist especially in urban areas where man-made structures like window corners lead to a strong and temporary stable radar return. Deformation analysis in urban areas based on a network of PS allows accuracies of few mm per year (Ferretti et al., 2001). We use Persistent Scatterers as the object representation of structures at a facade in the SAR data. The regularity of PS caused by structures like facades is reflected in an equidistant spacing of its forming elements (e.g. window corners) in SAR geometry (i.e. range, azimuth coordinate).

Figure 1 shows an example of a building complex with five clearly distinguishable facades. The SAR image of Figure 1(a) is overlaid with the PS as red dots. It strikes the eye that their two-dimensional alignment in the SAR geometry is not random. Rows along facade structures of the same height as well as regularities along consecutive levels are recognizable. Comparing these regularities with the oblique aerial image of Figure 1(b) makes obvious that the same kind of regularity can also be found in the alignment of windows at the facades on the one hand. But on the other hand, some PS seem to miss at positions which apparently do have the same correspondence in the optical image as positions which do have a Persistent Scatterer.

The fusion of SAR data to optical imagery needs a high level of abstraction due to the different imaging geometries. A common representation for facades are lattices which can be extracted in

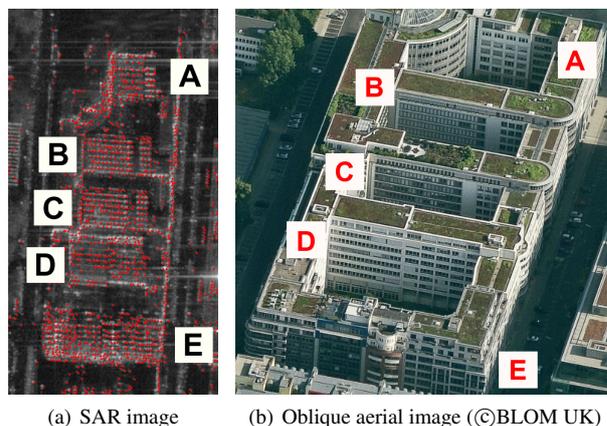


Figure 1: A building complex in the city center of Berlin in a SAR and oblique optical image. The regular facade patterns can be seen in both data types.

optical as well as in SAR data (Schack et al., 2012a). A lattice is given by the following form:

$$P_{nm} = nt_1 + mt_2 + t_3 \quad \text{with } n, m \in \mathbb{Z} \quad (1)$$

where t_1 and t_2 are the two lattice spanning vectors. t_3 is the origin of the lattice. The full integers n and m are bounded by the size of the lattice. Every position P_{nm} is one node of the lattice. Finding missing PS of the lattice than means to check all valid combinations of n and m . The validity in this case is simply given by the extension of the lattice. To determine the subset of PS belonging to regular facade structures means to conclude for all points if they are part of a lattice or not.

2 OBTAINING LATTICE TOPOLOGY INFORMATION BY GROUPING OF PERSISTENT SCATTERERS

Lattice Topology Information is the result of grouping Persistent Scatterers to lattices. The two spanning vectors of the lattice have to correspond to the vertical and horizontal alignment of the PS at the facade. There are several methods to extract lattices in PS point sets. One possibility is to model the human percep-

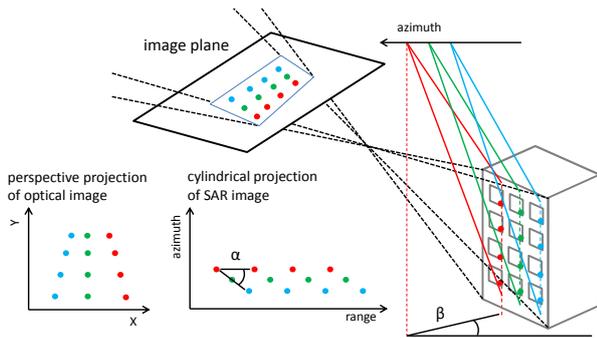


Figure 2: Sketch of the two different imaging geometries. Two important characteristics of the SAR mapping are exploited: a) Vertical aligned point scatterers are depicted into the same azimuth coordinate and b) rectangular patterns are depicted into a sheared rectangular.

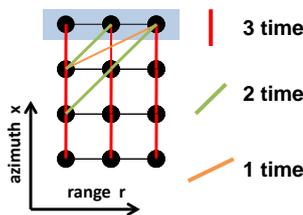


Figure 3: Schematic view of the counting algorithm to retrieve the lattice spanning vector corresponding to the horizontal alignment of PS in a regular alignment. The blue shaded row does belong to PS with the same planimetric position. Counting all directions of rows going through points belonging to this row, yields the numbers on the right hand side.

tion of recognizing regular structures in an disorderly surrounding (Gestalt Theory). This theory defines rules which are used in a production system to aggregate points to rows which are then grouped to lattices (Schack et al., 2012b). We also exploit knowledge about the SAR imaging geometry. Figure 2 shows the optical and SAR imaging geometry schematically. Due to the fact that the SAR mapping can be seen as a cylindrical projection of the real world, vertical aligned objects are depicted into the same azimuth coordinate. Therefore PS belonging to windows of consecutive levels which have the same planimetric position but different height do have the same azimuth coordinate in the SAR geometry. The second characteristic which helps grouping the PS is that the cylindrical mapping is homeomorphic and therefore preserves the topology. The rectangular alignment of the PS at a facade is mapped into a sheared rectangular. The angle of shear α of the mapping is proportional to the angle between the facade's normal and the sensor's line of sight projected to the ground (angle β in Figure 2).

To obtain the lattice spanning vector corresponding to the horizontal alignment of PS at the facade we need a simple assumption: Given a facade with a regular alignment of its windows, we assume that every column does have the same number of windows. This assumption holds for the majority of facades which are big enough to extract lattices in the SAR geometry. We then use a straightforward algorithm which counts the number of rows with the same direction in SAR geometry of all PS belonging to a row with the same azimuth coordinate (see Figure 3).

In this paper we use a combined approach where the minimum description length (MDL) principle (e.g. (Barron et al., 1998)) is used to support the production system by evaluating the grouping result. The MDL principle aims at finding the most compressed

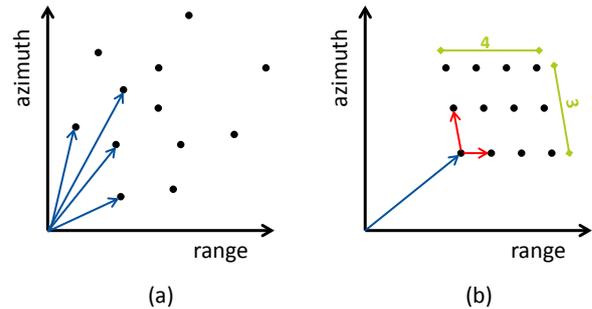


Figure 4: The MDL principle to evaluate the grouping of PS. (a) 12 randomly distributed PS. The proposed model simply stores all 12 two-dimensional coordinates. (b) 12 PS aligned in a lattice structure. The more sophisticated model describes the PS by the lattice' origin (blue), two spanning vectors (red) and two replication vectors (green) which define the size of the lattice.

description of all PS coordinates in SAR geometry. In short, this theory measures the coding length of a model and the data given this model to store the information. If there is any regularity in the data it can be exploited to define a combined model and data representation which has a shorter coding length and therefore a smaller description length. High regularity in the data corresponds to a short description length. Figure 4 illustrates this principle schematically. Imagine 12 randomly distributed points in a plane as in Figure 4(a). If there is no regularity at all, the smallest amount of data to describe this points is to directly store the coordinates. Assumed that storing a three-dimensional point with a defined precision would need C bit, the MDL is

$$MDL_a = 12 C \text{ bit.} \quad (2)$$

Given a pattern of 12 regular aligned PS, as in Figure 4(b), a more sophisticated model can be introduced to decrease the MDL. The lattice is then described by its origin (blue vector), two spanning vectors (red) and two replication numbers which define how often the spanning vectors are repeated to form the entire lattice (compare equation 1). Assuming that storing the replication numbers (e.g. two variables of data type integer) needs less information than storing a three-dimensional point (e.g. three variables with double precision), we see that describing the lattice needs only

$$MDL_b < 5 C \text{ bit.} \quad (3)$$

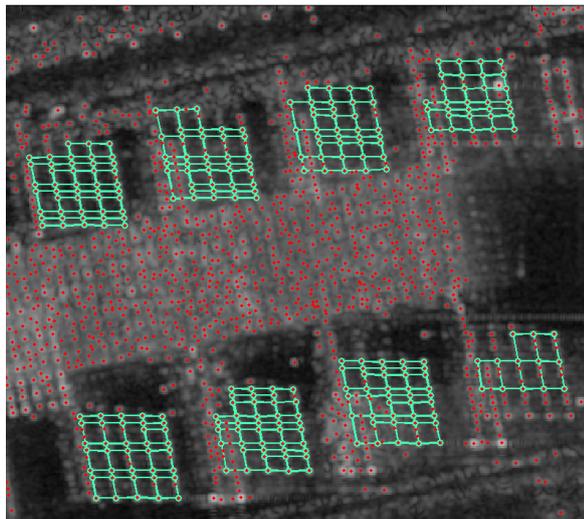
This simplified illustration of the MDL does not take into account the amount of information needed to code deviations of the true point positions with respect to their positions formed by equation 1. It also neglects the fact that storing the vector corresponding to the vertical alignment needs less information due to the exploitation of the SAR imaging geometry (compare Figure 2).

In our case we are interested in the geometrical regularity of three-dimensional points in the SAR geometry. Note, that the sketches in this paper only show two dimensions due to better readability. Figures 5 and 6 show results of the grouping algorithm.

Independently of the used method to aggregate the PS to lattices it is possible to infer missing points from already found nodes of the facade structure via predicting the two-dimensional position in SAR geometry and interpolating the height with help of the surrounding PS. In case of the production system we use a voting procedure. The grouping algorithm already calculates the direction and distance from one PS to its neighbours and tries to find other PS in the same directions but two times the distance from



(a) Oblique aerial image (©BLOM UK)

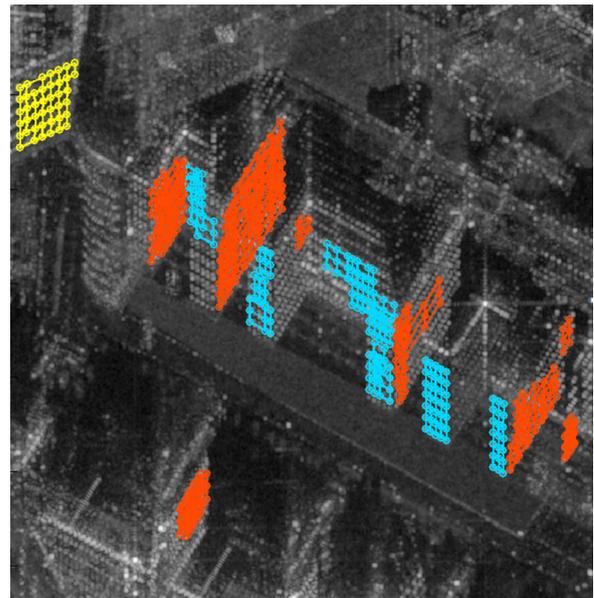


(b) SAR image

Figure 5: The Paul-Löbe-Haus in Berlin. The roof consists of concrete and glass. The resulting PS signature appears randomly. No lattice can be extracted. At the facades lattices can be aggregated.



(a) Oblique aerial image (©BLOM UK)



(b) SAR image

Figure 6: The building complex Park Kolonnaden in Berlin. The SAR image is flipped to facilitate the comparison with the optical image. The color of the lattices codes the orientation of the facade's normal with respect to the sensor's line of sight.

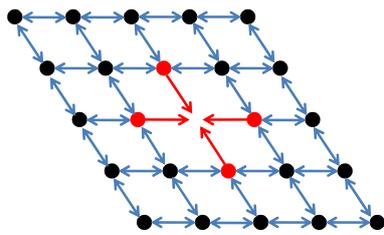


Figure 7: Principle of inferring missing PS from the local neighbourhood.

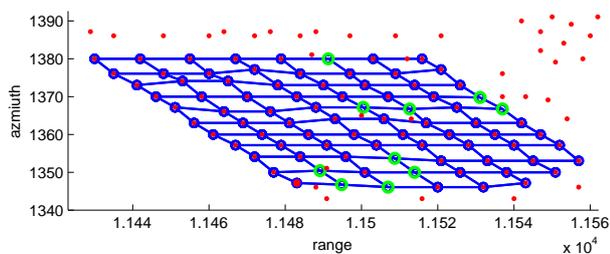


Figure 8: Lattice in SAR geometry. The red dots are Persistent Scatterers. Blue shows the aggregated lattice structure obtained by our production system approach. The green circles mark gaps in the lattice structure where no valid PS could be found in the neighborhood of the corresponding lattice position.

the originating point. Therefore the prediction of possible PS positions is system intrinsic. If a PS at a predicted position can be found it is added to a row of PS and later aggregated to a lattice. If no PS can be found, the predicted position is stored. The voting takes then place over all binned positions where no PS could be found. Figure 7 shows this procedure schematically. The PS in the middle is missing and the four neighboring PS (red) vote for that position. The binning can either be performed by simple thresholding the three-dimensional predicted positions or the lattice topology can directly be exploited by using equation 1 for all valid n and m . In the example of figure 7 the inference of PS A, B, C and D would lead to a voting of 4 for the missing point if the distance of their predicted positions would be smaller than the threshold. Setting the threshold depends on the resolution of the SAR stack and the typical spacing of windows at a facade.

Figure 8 shows an example of PS aggregated to a lattice by a production system as described in (Schack et al., 2012b). The green circles mark lattice positions in which neighborhood no valid PS could be found. Only PS are added to the lattice that have valid geocoded coordinate distances to its lattice neighbors. The validity depends also on the mentioned threshold. Furthermore model knowledge can be introduced by forcing the planimetric position of vertical aligned PS to be the same and horizontally aligned PS to have the same height. The geocoded positions are then improved in a common adjustment using the above mentioned geometrical constrains.

3 EXTRACTING LATTICES IN OBLIQUE AERIAL IMAGES

In order to unveil the physical nature of Persistent Scatterers we extract lattices in optical images and aim at matching them to the lattices extracted in PS point sets. Facades in oblique aerial imagery are represented as dense matrices of colored or gray scaled pixel values. Single objects of the facades like window corners can be found via simple corner detectors like the very often used by Harris (Harris and Stephens, 1988). To form those

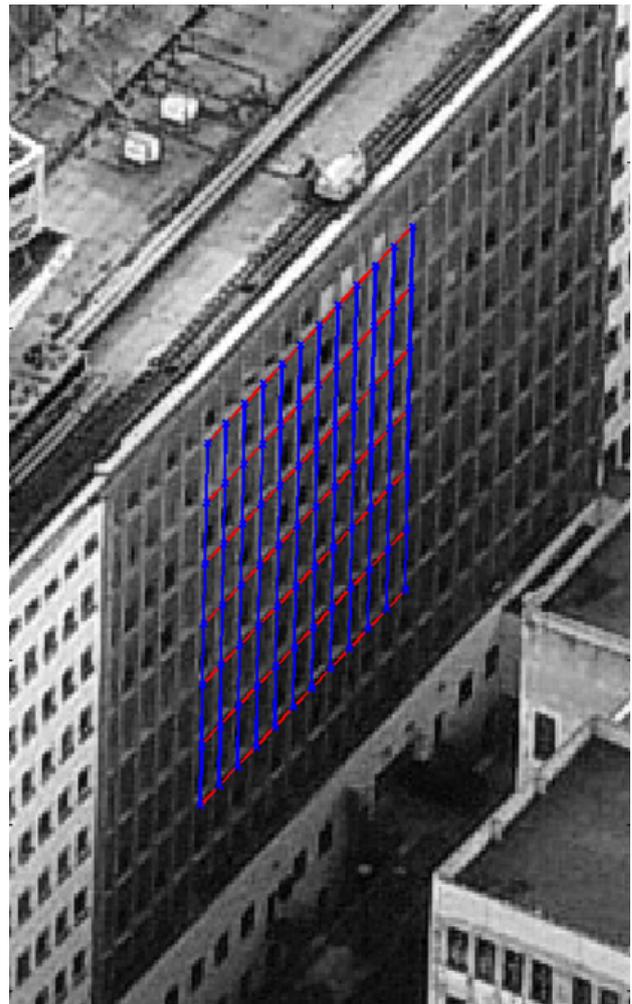


Figure 9: Result of lattice extraction in oblique optical image. The red vector correspond to the horizontal, the blue to the vertical alignment of the lattice nodes.

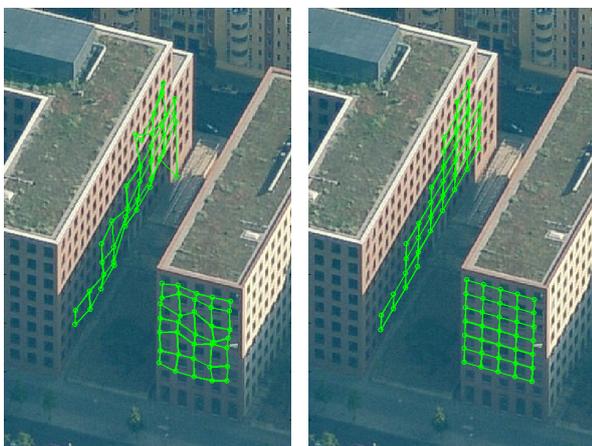
points to lattices we adopted an approach described in (Schindler et al., 2008). The key idea is that all point positions of any shear mapped lattice are integer values if an arbitrary subset of three L-forming adjacent points of this lattice is located on integer positions as well. As a first step a clustering of the Harris points is needed to separate different corners of the same object (e.g. the four corners of a window). For every cluster of the extracted Harris points, we randomly draw one point and perform an affine mapping of the two closest L-forming neighbors onto a regular $(0, 0); (1, 0); (0, 1)$ -grid. All points of the cluster are transformed with these parameters. If the transformed position of a point falls on an integer value (including a small tolerance) this point votes for the lattice candidate which is defined by the randomly drawn L-shape. The drawing is repeated several times and the three L-forming points with the majority of votings selected. Figure 9 shows an example of a lattice extracted in an optical image with this approach.

4 USING LATTICE TOPOLOGY INFORMATION

Under known conditions it can be assumed that the same parts of a building structure cause PS in the same manner and independently of their positions at the building structure (Schunert and Soergel, 2012). Simply spoken: if one window corner causes a PS, it is highly likely that neighboring window corners also lead to PS. This is valid as long as the structure that causes the PS



Figure 10: Lattice in oblique aerial image. Red: geocoded lattice; nodes are PS found in SAR geometry. Green: lattice positions without corresponding PS. The line of sight of the SAR sensor is roughly identical with the viewing direction of the airborne camera.



(a) Without geocoding adjustment. (b) With geocoding adjustment.

Figure 11: Improvement of two facades at site Park Kolonnaden, Berlin

does not change its appearance between the SAR acquisitions. Another reason for missing PS in a lattice is occlusion. Parts of buildings or other objects can be situated between the sensor and the object.

Figure 10 shows the geocoded and adjusted lattice of Figure 8 projected into an oblique aerial image. The green circles mark lattice positions where no valid PS in the SAR geometry could be found. In the optical image no evidence can be seen what prevents the corresponding window corner to cause a PS.

5 CONCLUSION AND OUTLOOK

We showed how lattice topology information can be deduced by aggregating single PS to lattices. The grouping algorithm uses a Production System and evaluates the results with the Minimum Description Length Principle. The lattice topology information helps to improve the geocoding of PS-lattices which is an important step in the process of matching them to lattices extracted in oblique optical imagery. The lattice topology information also helps directly the interpretation of SAR images.

At the moment we only use the MDL principle to evaluate the

grouping result. The lattice forming production system which produces the lattice candidates still uses a parameter to decide whether two predicted positions are the same or not. In future work we aim at replacing this threshold with a complete MDL framework to group the lattices in the SAR data. A big distance of the two predicted positions would correspond to a longer coding length. The MDL approach would therefore penalize big thresholds. Also the occurrence of gaps in a lattice structure could be coded in the MDL approach. Filling the gap could then decrease the MDL value.

Another important step towards the lattice matching is to define the matching framework itself. Due to the different imaging processes, the lattices have different geometric accuracies and also the number of columns and rows can be different. This leads to many challenges but also great potentials.

ACKNOWLEDGEMENTS

We gratefully thank Ralf Schroth from BLOM Romania SRL and Jason Crossley from BLOM UK for providing the oblique aerial imagery. We also thank Dr. Stefan Gernhardt and the Lehrstuhl für Methodik der Fernerkundung, TU München, for the PS point set.

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